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Self-assembled 3D photonic crystals from ZnO colloidal spheres

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9 Abstract

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We present a novel method for the controlled synthesis of monodisperse ZnO colloidal spheres. These spheres are self-assembled into fcc periodic arrays. Optical measurements, including reflection-mode optical microscopy and transmission and single-domain reflection spectroscopy, reveal that the periodic arrays exhibit a photonic band gap in the (1 1 1) direction of the fcc lattice, and calculations are presented to estimate the effective value of the refractive index of the colloidal spheres. Finally, photoluminescence (PL) measurements show that the ZnO lasing thresholds are lower in periodic structures than in random arrays of identical spheres.

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18 1. Introduction

Photonic crystals show a great deal of promise for appli-19 cations in numerous types of devices in 1, 2, and 3D struc-20 tures. The simplest devices are 1D structures consisting of 21 alternating layers of high- and low-index materials. By care-22 fully selecting the thickness of the alternating layers and the 23 refractive indices of the materials, the structure can be engi-24 neered to reflect a selected range of wavelengths. Structures 25 of this type form the basis for numerous devices including 26 dielectric mirrors and vertical-cavity surface-emitting lasers 27 [1]. 28

2D structures show promise for integration on silicon. 29 One significant problem with the evolution of photonic inte-30 31 grated devices is the ability to produce waveguides that can efficiently move photons across the surface of a chip. Specif-32 ically, traditional waveguide designs cannot include sharp 33 bends without significant signal loss. 2D waveguide struc-34 tures consisting of periodic 2D arrays of columns of a di-35 electric material have been demonstrated in which light can 36 37 be efficiently guided around a 90° bend [2]. In addition to passive devices such as waveguides, there is also significant 38 interest in devices formed from 2D periodic structures in 39 optically active materials. Some research has demonstrated 40 that it is possible to form a 2D defect-mode photonic band 41 42 gap laser in an InGaAs thin film system. A photonic crystal 43 is formed in the active layer by etching a periodic array of

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holes in the film. A defect is intentionally introduced into44the photonic crystal which acts as a laser cavity, and pro-45vides the opportunity for coherent feedback [3].46

A great deal of work is also underway in the area of 3D 47 photonic crystals. Numerous techniques have been devised 48 in an effort to produce periodic arrays of dielectric materials 49 that can exhibit a photonic stop band. Some synthetic tech-50 niques are quite elaborate including complex, multi-layer 51 lithography [4], multi-beam holographic lithography [5], op-52 tical interference methods [6], and production of so-called 53 inverted opal structures [7,8]. One of the simplest tech-54 niques, however involves colloidal self-assembly [9-11]. Es-55 sentially, monodisperse colloidal spheres will spontaneously 56 assemble into periodic arrays under certain circumstances. 57 Self-assembly does have some limitations; for example, col-58 loidal spheres typically arrange into a close-packed FCC 59 array, while it has been calculated that a diamond lattice 60 would be more likely to produce an omnidirectional pho-61 tonic band gap [12]. Also, thus far, most of the work per-62 formed in the area of self-assembled 3D photonic crys-63 tals has involved a few materials which are readily avail-64 able as monodisperse colloidal spheres in sizes appropri-65 ate for photonic crystals including SiO₂ and polymers, such 66 as polystyrene and PMMA. While these materials do prove 67 easy to assemble into FCC periodic arrays [11], their re-68 fractive indices are relatively low. In addition, while some 69 studies have been performed in which emissive materials are 70 added to the photonic crystal matrix [8,10,13], no work has 71 explored the properties of photonic crystals formed directly 72 from optically active materials. 73

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Clearly, there is a great deal of novel work that can 74 be performed in the area of self-assembled 3D photonic 75 crystals simply by choosing different material systems. Van 76 Blaaderen et al. have produced a number of interesting emis-77 sive materials as monodisperse colloidal spheres includ-78 ing Er^{3+} -doped SiO₂ [14], dye-doped PMMA [15], and 79 SiO₂/ZnS core/shell structures [16]. ZnO is another promis-80 ing candidate for optically-active self-assembled photonic 81 crystals because of its interesting optical properties. First, 82 ZnO has a higher refractive index (2.1–2.2 in the visible 83 regime) than other materials (1.4-1.5 for SiO₂ and most 84 polymers). In addition, ZnO has been found to be an ef-85 ficient emitter, exhibiting lasing behavior in the near UV 86 $(\lambda \sim 385 \, \text{nm})$ [17]. 87

In the current work, we describe 3D photonic crystals formed from ZnO colloidal spheres. We describe the synthetic process used to produce monodisperse ZnO colloidal spheres over a broad range of sizes, and the technique used to produce photonic crystals from these colloids. We also explore the optical properties of our photonic crystals.

94 2. ZnO colloidal sphere synthesis

The ZnO colloidal spheres used in this work were produced by a reaction similar to that described by Jezequel et al. [18]. ZnO was formed by hydrolysis of zinc acetate dihydrate (ZnAc). In a typical reaction, 0.03 mol ZnAc was added to 300 ml diethylene glycol (DEG). This reaction solution was heated under reflux to 160 °C. Shortly after reaching the working temperature, precipitation of ZnO oc-101 curred. Jezequel et al., reported that it was possible to pro-102 duce monodisperse ZnO powders of various sizes using this 103 method by changing the rate at which the reaction solu-104 tion was heated. They reported the production of spheres in 105 the narrow size range $0.2-0.35 \,\mu\text{m}$. Powders produced us-106 ing this technique in our lab, however, were typically widely 107 polydisperse with sizes ranging from ~ 100 to 1500 nm. 108

In our experiments monodisperse ZnO colloidal spheres 109 were produced by a two-stage reaction process. A primary 110 reaction was performed as described above, and the prod-111 uct was placed in a centrifuge. The supernatant (DEG, dis-112 solved reaction products, and unreacted ZnAc and water) 113 was decanted off and saved, and the polydisperse powder 114 was discarded. A secondary reaction was then performed to 115 produce the monodisperse ZnO spheres. The secondary re-116 action began in the same way as a primary reaction: 0.03 mol 117 ZnAc was added to 300 ml DEG and the reaction solution 118 was heated under reflux. Prior to reaching the working tem-119 perature, however, typically at 150 °C, some volume of the 120 primary reaction supernatant was added to the solution. Fol-121 lowing this addition, there was a temperature drop, and pre-122 cipitation would typically occur at a lower temperature than 123 without such an addition. After reaching 160°C, the reac-124 tion was stirred for one hour, after which the heat source 125 was removed, and the flask cooled to room temperature. 126

The scanning electron microscope (SEM) images in Fig. 1 127 reveal that the ZnO synthesized using this technique consists 128 of monodisperse colloidal spheres, and that the size of the 129 spheres varies inversely and monotonically with the amount 130

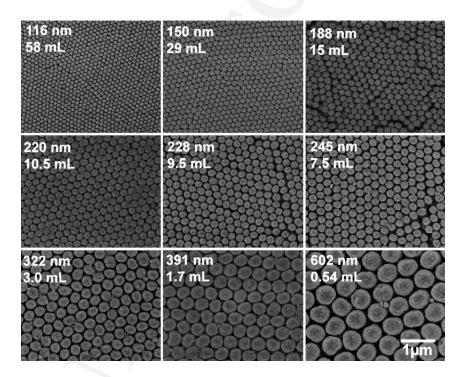


Fig. 1. SEM micrographs of monodisperse ZnO powders of various sizes produced using a two-stage hydrolysis. Numbers in the corners of the images indicate the mean sphere diameter and the amount of primary supernatant added.

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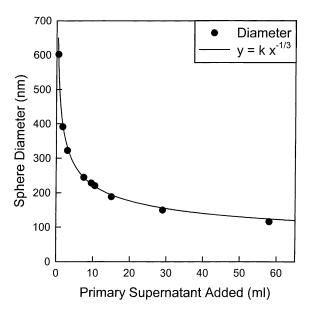


Fig. 2. Plot of the relationship between the amount of primary supernatant added and sphere diameter. Squares indicate real data, and the line is a fit of a function of the form $kx^{-1/3}$.

of primary supernatant added. Careful analysis of the mi-131 crographs reveals that the spheres formed are monodisperse 132 within 5-8%. Plotting sphere diameter as a function of pri-133 mary supernatant added reveals that the data fall very close 134 to a $kx^{-1/3}$ dependence, as can be seen from the solid line 135 in Fig. 2. This result provides a method to easily synthe-136 size monodisperse ZnO colloidal spheres over a broad size 137 range (\sim 100–600 nm), with good control over the diam-138 eter. We expect that it should be possible to extend this 139 method to produce particles larger or smaller than those that 140 have been synthesized thus far. As will be seen, however, 141 this range of sizes is adequate to create photonic crystals 142 with band gaps covering the entire visible spectrum and 143 extending well into the UV and IR. In addition to reveal-144 ing the sphere diameter, SEM also shows that the spheres 145 are made up of numerous nanocrystallites. X-ray diffraction 146 analysis of the colloid reveals that the material is hexago-147 nal ZnO with a crystallite size of 10-20 nm and no pref-148 149 erential growth direction. The transmission electron micrograph in Fig. 3 confirms the polycrystalline nature of the 150 spheres. 151

It should be noted that it is necessary to use the super-152 natant from the primary reaction to produce the monodis-153 perse colloidal spheres. If the ZnO is not removed from 154 the reaction solution, the polydisperse spheres from the pri-155 mary reaction mix with the monodisperse spheres from the 156 secondary reaction, disrupting the self-assembly of the pe-157 riodic arrays described later. Additionally, if pure DEG is 158 added as the nucleation agent, the product consists of poly-159 160 disperse ZnO spheres similar to that of the primary reaction. Furthermore, a "synthetic" primary reaction super-161 natant consisting of amounts of precursor (ZnAc) expected 162 to remain unreacted, and appropriate amounts of soluble re-163

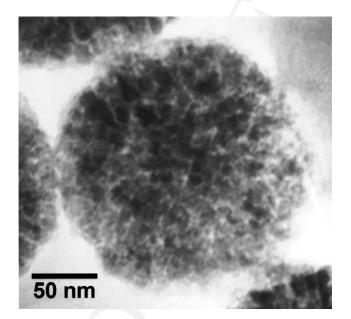


Fig. 3. TEM Micrograph of a single ZnO sphere showing nanocrystalline substructure of the material.

action by-products (acetic acid) failed to produce monodisperse ZnO spheres. 164

Photonic crystals were produced from the ZnO colloidal 166 spheres using a sedimentation self-assembly process. The 167 reaction solution was dropped onto a substrate typically at 168 160°C, and as the solvent evaporated, the particles spon-169 taneously assembled into periodic structures with domain 170 sizes typically in the range of several microns. Examples 171 of the structures observed can be seen in Fig. 1. Substrates 172 were chosen based upon application. For SEM, Si substrates 173 were used, and for optical measurements, glass substrates 174 were used. From optical microscopy, there is no difference 175 between layers formed on glass and those formed on Si. 176

Temperature plays an important role in the assembly of 177 periodic structures. A series of several samples of 245 nm 178 ZnO was prepared with sedimentation and drying tempera-179 tures ranging from 100 to 300 °C. It was noted that at low 180 temperatures, layers exhibited no periodicity observable in 181 SEM, and at high temperatures, the powder adhered poorly 182 to the substrate. The solvent also appears to play an impor-183 tant role in self-assembly. While layers sedimented from the 184 original reaction solution produce crystalline structures, lay-185 ers sedimented from other solvents including acetone, water, 186 and several alcohols produced no observable periodic struc-187 tures. This could be, in part, attributable to the lower boiling 188 points, and consequently lower sedimentation temperatures 189 required, when using solvents other than DEG. 190

Based on plan-view SEM, it is impossible to determine 191 whether the structure of the photonic crystals is FCC or 192 HCP. In order to determine the structure, cross-sectional 193 SEM samples were prepared, and the edge of the layer was 194 observed. An FCC structure was confirmed by the presence 195 in all samples of (100) square-lattice planes. In addition, it 196

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was observed that the thickess of the layers, while variable 197 across the surface of the sample, has an average value of 198 approximately 2-3 µm, corresponding well with thicknesses 199 calculated from expected yields. Unfortunately, it proved 200 difficult to observe photonic crystal properties for layers this 201 thin, particularly for films of larger particles that may consist 202 of only 3-4 monolayers. In order to produce thicker layers, 203 the reaction solution was concentrated. The as-synthesized 204 solution was placed in a centrifuge, and the powder was 205 allowed to settle to the bottom. Some fraction (typically 206 85-90%) of the liquid was then removed, and the powder 207 was redispersed by sonication. A single drop placed on a 208 heated substrate would then result in a much thicker, but still 209 periodic structure. 210

211 3. Optical characterization

Several types of measurement were performed in order 212 to characterize the photonic band gap structures in the peri-213 odic ZnO arrays. Reflection-mode optical microscopy was 214 used to observe the general color of the reflected light, large 215 area transmission measurements were performed to detect 216 the presence of a photonic stop band, and spatially-resolved 217 reflection spectroscopy was performed to evaluate the qual-218 ity of individual domains. In addition, we have performed 219 simulations to evaluate the photonic band structure of our 220 crystals. 221

Using normal-incidence transmission spectroscopy, it was easy to observe band gaps for our periodic structures. The size range of our colloidal spheres resulted in band gaps covering the entire visible part of the spectrum, and are expected to extend from the UV to the IR. Plots of the transmission results and their corresponding particle sizes can be seen in Fig. 4. Table 1 lists the mean sphere diameters,

Table 1	
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Relationship	between ZnO	sphere diameter and	photonic band	gap position

<i>d</i> (nm)	λ (nm)	d/λ
116	257	-
150	333	_
188	433	0.433
220	487	0.452
245	538	0.455
322	700	0.460
391	865	0.452
602	1336	_

the observed wavelength of the corresponding photonic band 229 gap, and the ratio of particle size to wavelength (d/λ) . The 230 ratio is constant to within a few percent over all samples. The 231 lighter values in Table 1 correspond to samples whose gap 232 is not observed, but is expected to lie either outside of the 233 range of the spectrometer or beyond the absorption edge of 234 ZnO. It should also be noted that the colors corresponding to 235 the band gaps observed are clearly visible in reflection-mode 236 optical microscopy. 237

While transmission is an effective technique for detecting 238 the presence and location of a photonic band gap, it is diffi-239 cult to quantify the width of the gap because it measures a 240 large area of the sample which may include many different 241 periodic photonic domains, as well as areas of disorder and 242 areas where no material is present. In order to better char-243 acterize the photonic band gap, spatially-resolved reflection 244 spectroscopy was used [10]. Essentially, a white light source 245 was focused onto the surface of the sample using a micro-246 scope objective lens. The image of the sample was then pro-247 jected on the entrance slit of a spectrometer. Images of the 248 spectrometer CCD were taken, with one dimension corre-249 sponding to wavelength and the other corresponding to real 250 space on the surface of the sample. By selecting a few lines 251

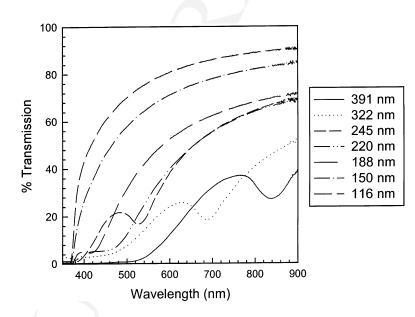


Fig. 4. Transmission spectra for periodic layers of ZnO spheres of various sizes.

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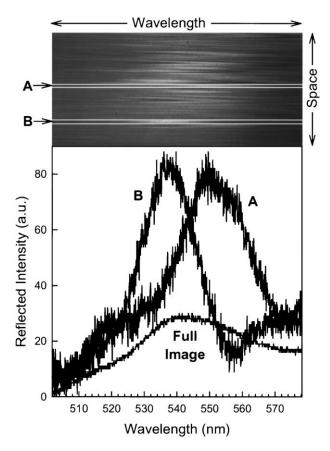


Fig. 5. Spectrometer CCD image and corresponding plots for reflection spectroscopy of a 245 nm ZnO powder structure. Letters beside the image indicate the CCD location from which the corresponding curves in the plot were constructed.

from the spectrometer CCD corresponding to single domains 252 on the surface of the sample, it is possible to get a better 253 measure of both the position and the width of the photonic 254 band gap. Fig. 5 shows a typical spectrometer CCD image 255 for a layer of 245 nm ZnO colloidal spheres and spectra cor-256 responding to both the full image and two single-domain 257 bands. While transmission measurements result in a FWHM 258 of 60-80 nm, and large area reflection measurements show 259 260 a width of approximately 40 nm, single-domain measurements result in a spectral width of approximately 20 nm or 261 about 4%. It is believed that the broadening of the band gap 262 in large-area cases results from the addition of numerous 263 domains that may have slightly different orientations and 264 therefore slightly different reflection maxima. This is clear 265 266 from the different positions of the two single-domain plots show in Fig. 5. 267

To support our optical measurements we have also performed band structure calculations. Using a block-iterative, frequency-domain method [19] for Maxwell's equations (in a plane-wave basis) we calculated the band structure for 3D FCC lattices of dielectric spheres with indexes of refraction varying between 1.2 and 3.0, and radius to interparticle distance ratios (r/d, a measure of the packing density of the spheres) from 0.2 to 0.6. To describe normal-incidence op-275 tical experiments, we restricted ourselves to the (111) di-276 rection of the FCC lattice. The results of these calculations 277 can be found in Fig. 6. Fig. 6a shows a plot of gap position 278 (d/λ) in the (1 1 1) direction and 6(b) a plot of the gap width 279 (%) normalized by the center frequency, each as a function 280 of refractive index and r/d. For a refractive index of 2.1 (ap-281 proximate bulk value for ZnO) the results indicate that d/λ 282 can be approximated as 0.35, while in our case the ratio 283 was close to 0.45. This discrepancy implies that the effec-284 tive refractive index of the photonic crystal structure differs 285 significantly from the bulk value. Packing density was esti-286 mated from SEM images to yield r/d in the 0.45–0.50 range. 287 Restricting the packing parameter to this interval, and keep-288 ing $d/\lambda = 0.45$ (bold segment on Figs. 6a,b), gives us an 289 effective index in the 1.5–1.7 range. This value is further 290 supported by the calculations of relative gap width. As can 291 be found in Fig. 6b, the width is predicted to lie between 292 5.5 and 7.8%. The value observed in our single-domain re-293 flection measurements, approximately 4%, is smaller than 294 the above prediction. This reflects the presence of the resid-295 ual disorder, inevitable in the experimental photonic crystal 296 structures studied here. 297

The fact that the refractive index is lower than the bulk 298 value is most likely the result of low density in the powders. 299 Jezequel et al., found that ZnO spheres produced by the hy-300 drolysis of ZnAc are highly porous [18]. It may be possible 301 to increase the refractive index by annealing the powders to 302 increase their density, or by filling in the pores with SiO₂ 303 in a technique similar to that described by Velikov and van 304 Blaaderen [16]. 305

In addition to the optical measurements used to charac-306 terize the photonic band gap, photoluminescence (PL) mea-307 surements were also performed to observe the emissive prop-308 erties of the colloidal spheres. In these measurements, a 309 pulsed, frequency-tripled, Nd: YAG laser emitting at 355 nm 310 at 10 Hz with a pulse length of approximately 20 ps was 311 used as the pump source. The beam was focused to a spot 312 approximately 25 µm in diameter on the surface of the sam-313 ple. The PL system was set up with a white light source and 314 a CCD camera to observe the samples and select a clean 315 area on the surface for measurement. In addition, the sample 316 could be viewed after the PL experiments were complete to 317 see if any damage had been caused by the pump source. 318

For the lasing measurements, 16 samples were prepared 319 comprising periodic and random structures in each of eight 320 different colloidal sphere sizes. All samples exhibited las-321 ing type behavior, detectable by the evolution of narrow 322 peaks in the emission spectrum. For each sample, several 323 locations were measured, and the value of the lasing thresh-324 old was recorded. In all cases, periodic structures showed 325 a lower lasing threshold by a factor ranging from ~ 1.5 to 326 4.0 with an average value of approximately 2.5. This behav-327 ior is likely due, at least in part, to a higher sphere packing 328 density in the periodic structures. In future work, we plan to 329 produce a photonic crystal in which the position of the pho-330

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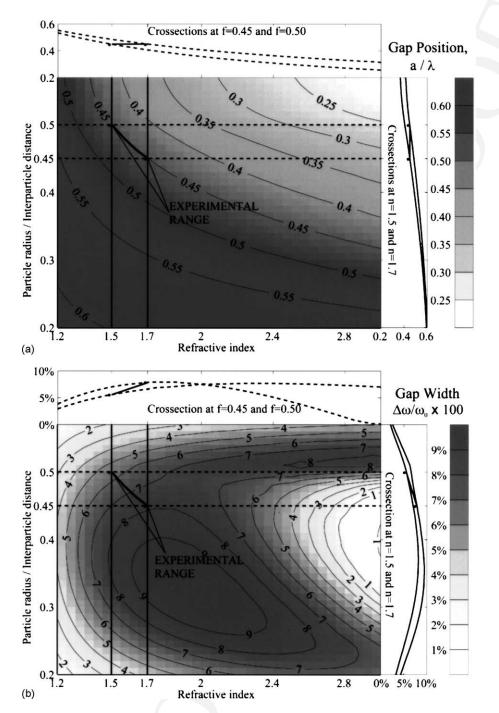


Fig. 6. Results of photonic band calculations. (a) Gap position (d/λ) and (b) gap width (%) as a function of refractive index and packing density.

tonic band gap overlaps the ZnO emission spectrum which
we expect will demonstrate a significantly higher lasing
efficiency.

334 4. Conclusions

In summary, we have developed a technique to produce monodisperse ZnO colloidal spheres. Our technique employs a two-step reaction, and allows close and predictable control of the size of the spheres during the secondary reaction by varying the amount of primary reaction supernatant 339 added. We have demonstrated the production of particles 340 ranging in size from ~ 100 to 600 nm, and believe that it 341 should be possible to go beyond this range. 342

We have self-assembled periodic arrays of these colloidal 343 spheres by dropping the reaction solution onto substrates 344 and evaporating the solvent. We have found that ordering 345 only occurred at relatively high substrate temperatures, and 346 no ordering could be observed when the reaction solvent 347

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was exchanged for other solvents such as water, acetone, or 348 alcohols. 349

It has been found that the periodic arrays of the powder 350 exhibit a photonic band gap in the fcc (111) direction at 351 approximately 2.2d where d is the mean particle diameter. To 352 our knowledge, this is the first demonstration of 3D photonic 353 crystals in ZnO. 354

Finally, we have performed photoluminescence mea-355 surements on random and periodic arrays of layers of our 356 monodisperse colloidal spheres. We have found that the 357 ZnO colloidal spheres are optically active, and capable of 358 exhibiting laser-like behavior. It is found that the lasing 359 threshold in periodic structures is lower than that in random 360 structures by a factor of approximately 2.5. 361

Because of ZnOs unique optical and lasing properties, this 362 work opens up many unique and exciting research opportu-363 nities previously unavailable in the area of self-assembled 364 3D photonic crystals. 365

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